

# CBMC-GC: Secure Two-Party Computations in ANSI C



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# Data Privacy — The Traditional Approach

Data privacy relies on several technical and administrative approaches:

- Legal requirements
- Policies
- Audits
- Training
- Technical means (access control, network security, intrusion detection)
- Physical security

# Does it work?



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## Restaurant chain customers' credit card data stolen

The Boston Globe

By Bruce Mohl, Globe Staff | October 1, 2007

Not Your Average Joe's, a Massachusetts restaurant chain, said yesterday that thieves have stolen credit card information from its customers.

The Dartmouth-based chain estimated less than 3,500 of the 350,000 customers it served in August and September had their credit card information stolen. The 14-restaurant chain said it is working with the US Secret Service and major credit card companies to determine how the data theft occurred and precisely how many customers were affected.

Today, the chain plans to post on its website a notice to customers about the security breach.

Diana Pisciotta, a spokeswoman for Not Your Average Joe's, said the chain decided to check their credit card statements with companies about any suspicious charges but not responsible for fraudulent activity on them.

"We're doing this out of an abundance of caution and forthright with our customers," she said.

## Stolen computer contained info from 88,000 patients at Staten Island hospital

by Staten Island Advance  
Wednesday April 30, 2008, 4:37 PM

Computer equipment [stolen from an administrative office in Clifton in December](#) contained personal information from 88,000 patients that have been treated at Staten Island University Hospital.

After four months with no arrests, hospital administrators are just now beginning the process of sending out letters to patients whose names, Social Security and health insurance numbers were contained in computer files on a desktop computer and a backup hard drive stolen Dec. 29 from the hospital's finance office at 1 Edgewater Plaza.

"The hospital is in the process of issuing a statement to each patient involved in which one year of financial records will be included in a hospital statement, released by spokeswoman said.

News Site of the Year | The 2008 Newspaper Awards

## TIMES ONLINE

NEWS COMMENT BUSINESS SPORT LIFE & STYLE ARTS & ENTERTAINMENT RICH LIST

UK NEWS WORLD NEWS POLITICS ENVIRONMENT WEATHER TECH & WEB NEWS RELATED

Where am I? > Home > News > Politics

From The Times

January 19, 2008

## Personal data of 600,000 on lost laptop



Michael Evans, Defence Editor

A junior Royal Navy officer is facing a court martial after a laptop containing the personal data of 600,000 people, including serving personnel and thousands of people who have shown an interest in a military career, was stolen from his car.

The loss of the laptop was considered to be so serious that Des Browne, the Defence Secretary, will make a statement to the Commons early next week.

### TIMES RECOMMENDS

- > MPs back creation of human-animal embryos
- > Bank Holiday plan to celebrate Armed Forces
- > Wanted: criminal law expert to be new DPP

### EXCLUSIVE EXTRACTS



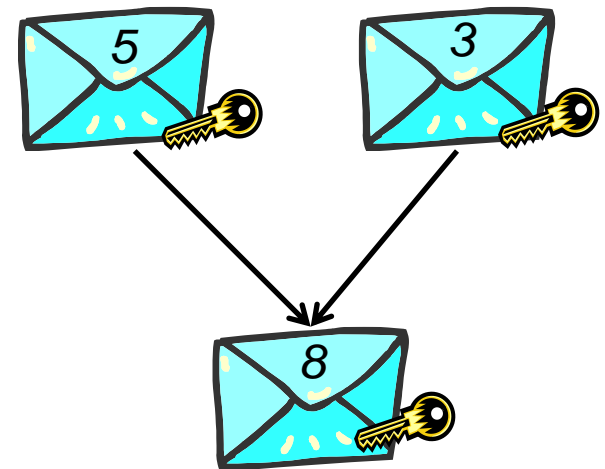
### Cherie autobiography

Full coverage and exclusive interviews and extracts from a decade in power

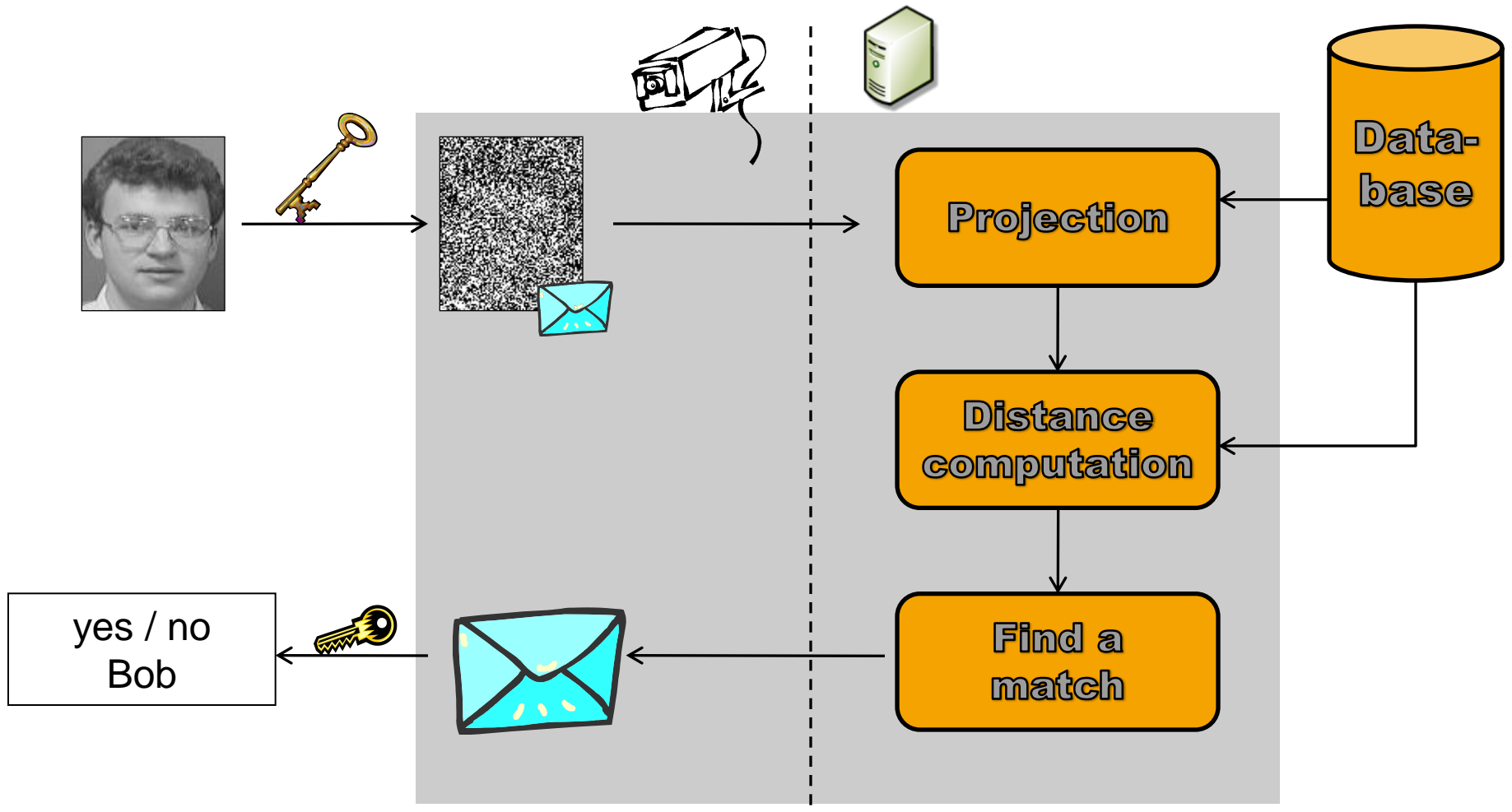
# Privacy-Enhancing Technologies (PETs)

- Strike a balance between data availability and privacy
- **Paradigm:** keep data encrypted, PETs **compute with encrypted data**
- **Privacy By Design:**  
Cryptographic protocols precisely limit amount of information available

- Cryptographic tools are available!
  - Homomorphic encryption
  - Yao's Garbled circuits
  - Customized protocols (private set intersection, ...)



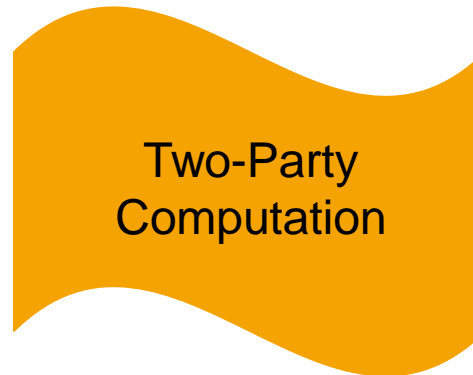
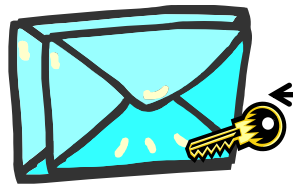
# Example: Private Face Detection



# Example: Private Processing of Genome Data

Physician

Bioinformatics Institute



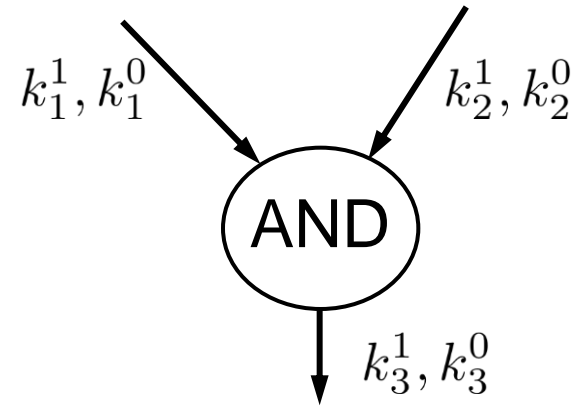
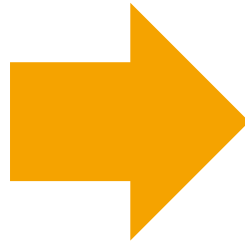
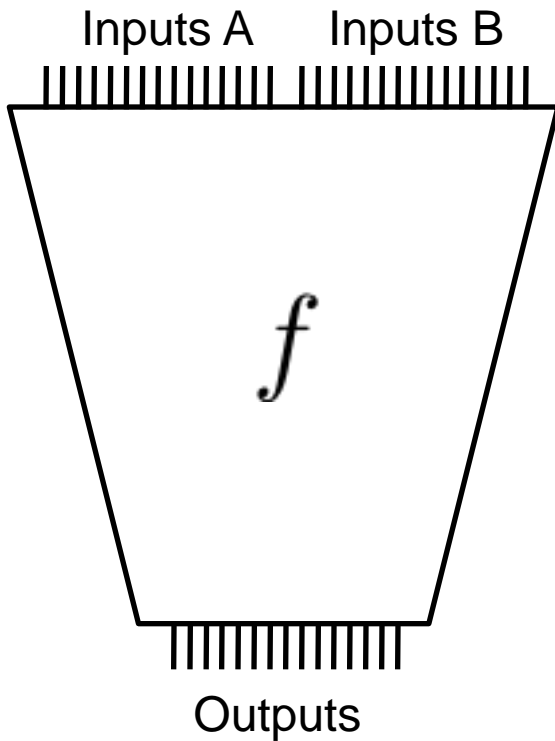
*Medical  
Test*



# Nice approach, but is it ready for practice?

- Cryptographic protocols are ready, **but tedious to use**
- Lack of a good tool chain that a programmer can use
- Research prototypes are available:
  - Fairplay, FairplayMP, Sharemind, Tasty
  - Fast GC frameworks (implementation support for Java)
- We need “usable” **compilers** that helps a programmer implement PETs!

# Recap: Yao's garbled circuits



$\wedge$	$x = 1$	$x = 0$
$y = 1$	1	0
$y = 0$	0	0

	$x = 1$	$x = 0$
$y = 1$	$E(k_1^1, E(k_2^1, k_3^1))$	$E(k_1^1, E(k_2^0, k_3^0))$
$y = 0$	$E(k_1^0, E(k_2^1, k_3^0))$	$E(k_1^0, E(k_2^0, k_3^0))$



# Our choice as basis: Bit-precise Model Checker CBMC

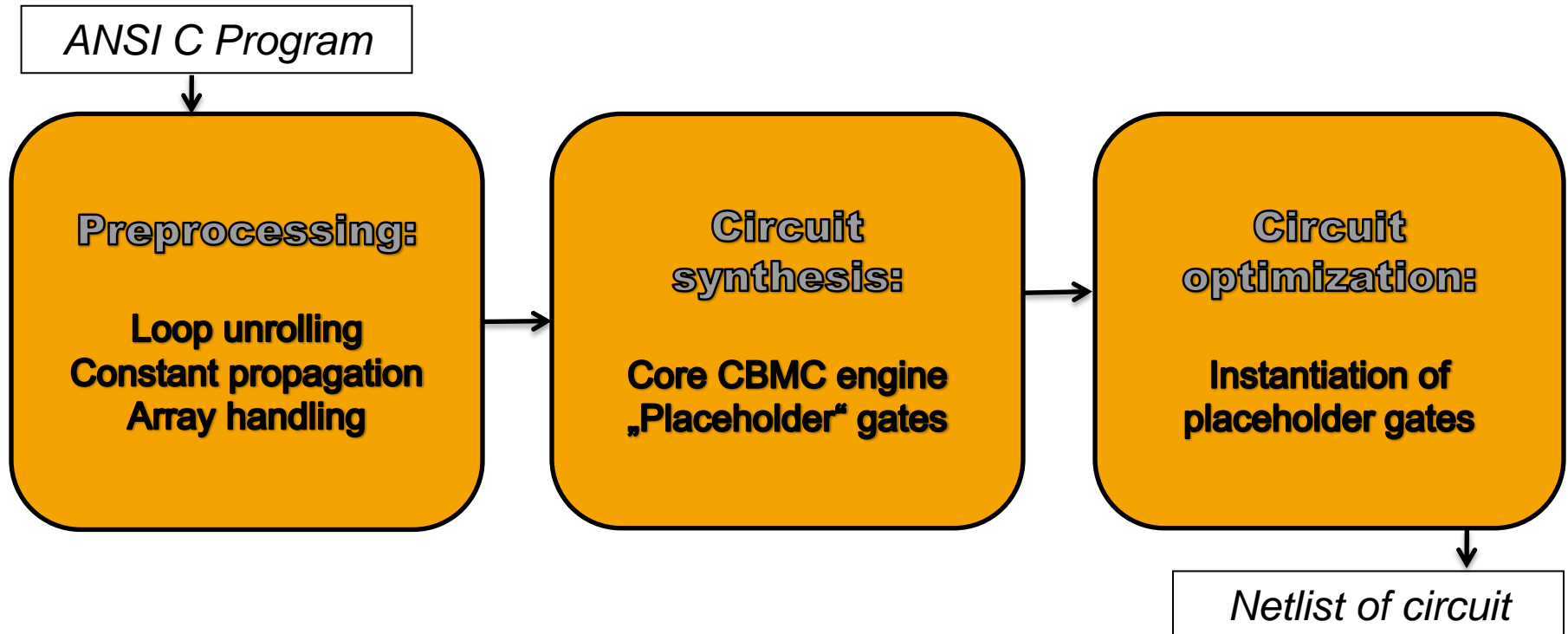
- Transforms C program into a Boolean formula
- Transformation is “bit precise”
  - ➔ models evolution of program memory



<http://www.cprover.org>

- **Bounded model checker:**
  - Unrolls program up to a fixed number of loop iterations
  - Heuristics on how much unrolling is needed
- Boolean formula consists of program model and negated property
- SAT solver checks for solution


**Central idea:** use transformation from C code to SAT  
formula provided by CBMC for secure computing



# CBMC-GC: Example, Yao's Millionaires

```
void millionaires() {  
    int INPUT_A_mila;  
    int INPUT_B_milb;  
    int OUTPUT_res;
```

Local variables code  
inputs and outputs



```
    if (INPUT_A_mila > INPUT_B_milb)  
        OUTPUT_res = 1;  
    else  
        OUTPUT_res = 0;  
}
```

Computations  
specified as C program



# CBMC-GC: A bigger example

## Matrix multiplication

```
#define S 8 // size of matrices
```

```
int INPUT_A_a[S][S];
```

```
int INPUT_B_b[S][S];
```

```
int OUTPUT_c[S][S];
```

```
void multiply()
```

```
{
```

```
    int i, j, k;
```

```
    for (i = 0; i < S; i++)
```


```
        for (j = 0; j < S; j++)
```

```
            for (k = 0; k < S; k++)
```

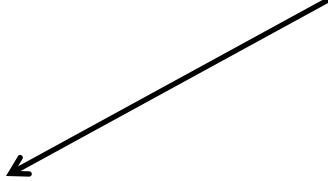
```
                OUTPUT_c[i][j] += INPUT_A_a[i][k] * INPUT_B_b[k][j];
```

```
}
```

More complex data types  
like arrays, structs, enums



(Limited) support for  
pointer arithmetic



# Limitations

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CBMC-GC inherits limits from CBMC:


- **Bounded programs:** bounds for all loops must be known  
→ in practice no problem
- No support for **floating point arithmetic**
- No support for **library functions** (yet)
- Limited **pointer arithmetic**
- **Integer data types** of fixed size  
→ limits efficiency in secure computations

# CBMC-GC: More examples

## Bubblesort

```
#define K 11 // length of array
#define MEDIAN 5 // position of median
int INPUT_A_a[K];
int OUTPUT_median;
void median_bubblesort() {
    int i, j, tmp, tmp1, tmp2;
    for (i = K - 1; i > 0; i--) {
        for (j = 0; j < i; j++) {
            tmp1 = INPUT_A_a[j]; tmp2 = INPUT_A_a[j + 1];
            if (tmp1 > tmp2) {
                INPUT_A_a[j] = tmp2; INPUT_A_a[j + 1] = tmp1;
            }
        }
    }
    OUTPUT_median = INPUT_A_a[MEDIAN];
}
```

CBMC can determine  
loop bounds by static analysis




# CBMC-GC supports recursion

## Example: Mergesort

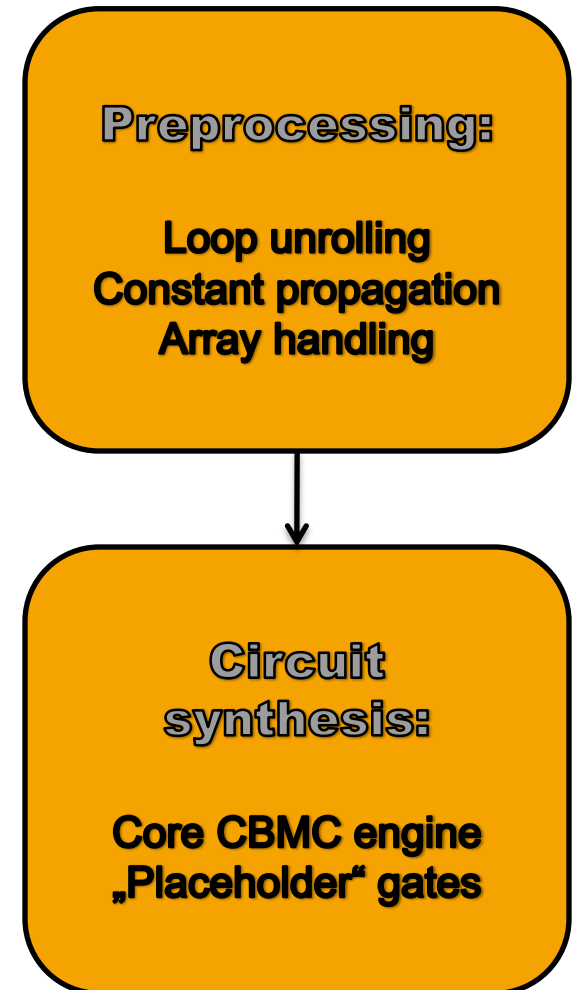
```
int b[K]; // temporary array for mergesort
void mergesort(int l, int r) {
    int i, j, k, m;
    if (r > l) {
        m = (r + l)/2; mergesort(l, m); mergesort(m + 1, r);
        for (i = m + 1; i > l; i--)
            b[i - 1] = INPUT_A_a[i - 1];
        for (j = m; j < r; j++)
            b[r + m - j] = INPUT_A_a[j + 1];
        for (k = l; k <= r; k++) {
            if (b[i] < b[j])
                INPUT_A_a[k] = b[i]; i++;
            else
                INPUT_A_a[k] = b[j]; j--;
        }
    }
}
```

Recursion; CBMC can determine bounds by static analysis



# CBMC-GC: Optimizations

- Array access are slow
  - requires evaluation of a MUX circuit
  - remove some by static analysis
- CBMC is optimized for SAT performance
  - introduce placeholder gates
  - later instantiation with optimized circuits
- Optimization engine extensible





# Experimental results

We used CBMC-GC in conjunction with framework for execution of garbled circuits by Huang et al (USENIX 2011)

Experiment	Number of gates	Execution time, preprocessing	Execution time, circuit evaluation
3000 random arithmetic operations	2,298,441 (608,668)	970 ms	9,774 ms
8x8 matrix multiplication	3,257,345 (905,728)	680 ms	18,173 ms
Median, bubble sort, 31 elements	149,040 (45,120)	733 ms	1,644 ms
Median, merge sort, 31 elements	1,339,084 (436,916)	660 ms	3,790 ms

# Conclusions

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- Automatic compilation of two-party protocols is indeed possible
- Not as fast as hand-written code, but nevertheless usable in practice
- Will hopefully stimulate research in optimization issues, separates crypto functionality from compiler design
- Future research: other basic tools, other languages, optimizations, overcoming current limitations of CBMC-GC, ...



To come:

***<http://forsyte.at/software/cbmc-gc/>***